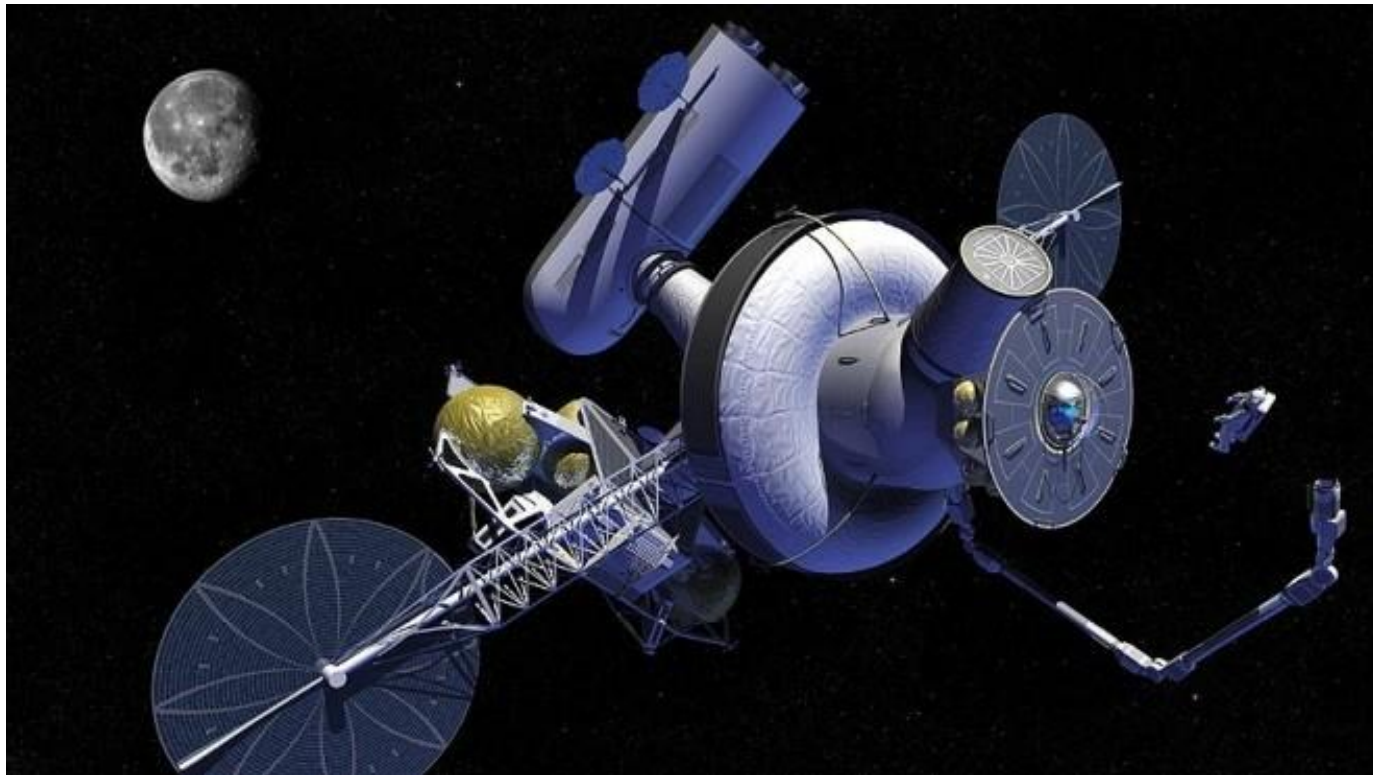




# Access to Mars from Earth-Moon Libration Point Orbits: Manifold and Direct Options



Masaki Kakoi  
Kathleen C. Howell  
David Folta

Suggested EML<sub>2</sub> module  
Image: NASA

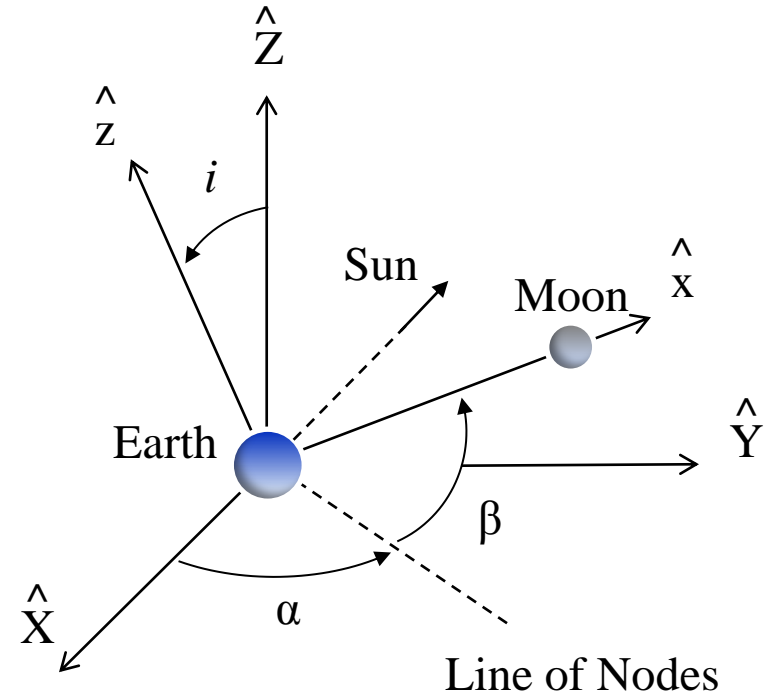
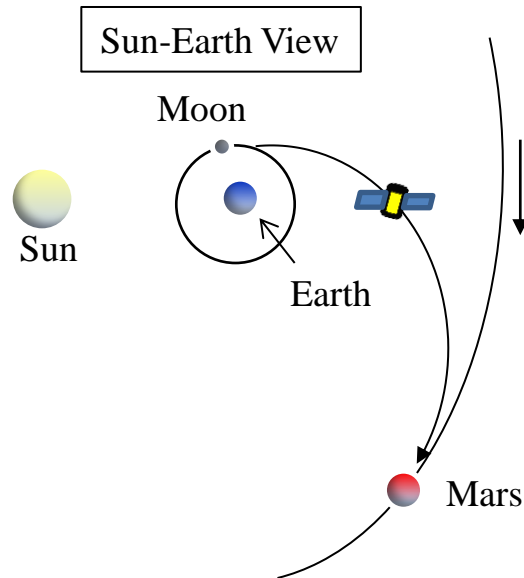


# Objectives

## Development of general procedure:

- Transfers from EM  $L_1/L_2$  halo orbits to Mars
  - System model
  - EM manifold transfers
  - SE manifold transfers
  - Direct transfers
- Transition to higher fidelity model

# System Model: Five-Body Problem

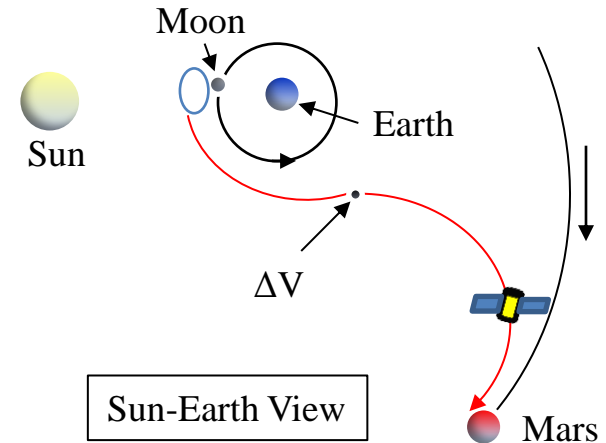


- Blended Sun-Earth-Moon model
  - Circular Restricted Three-Body Problems
  - Body two 3-1-3 Euler angle sequence
    - $\alpha$  : longitude of ascending node
    - $i$  : inclination  $5^\circ$
    - $\beta$  : argument of latitude
- Mars: Ephemeris location



# Scenario 1: Sun-Earth Manifold Transfers

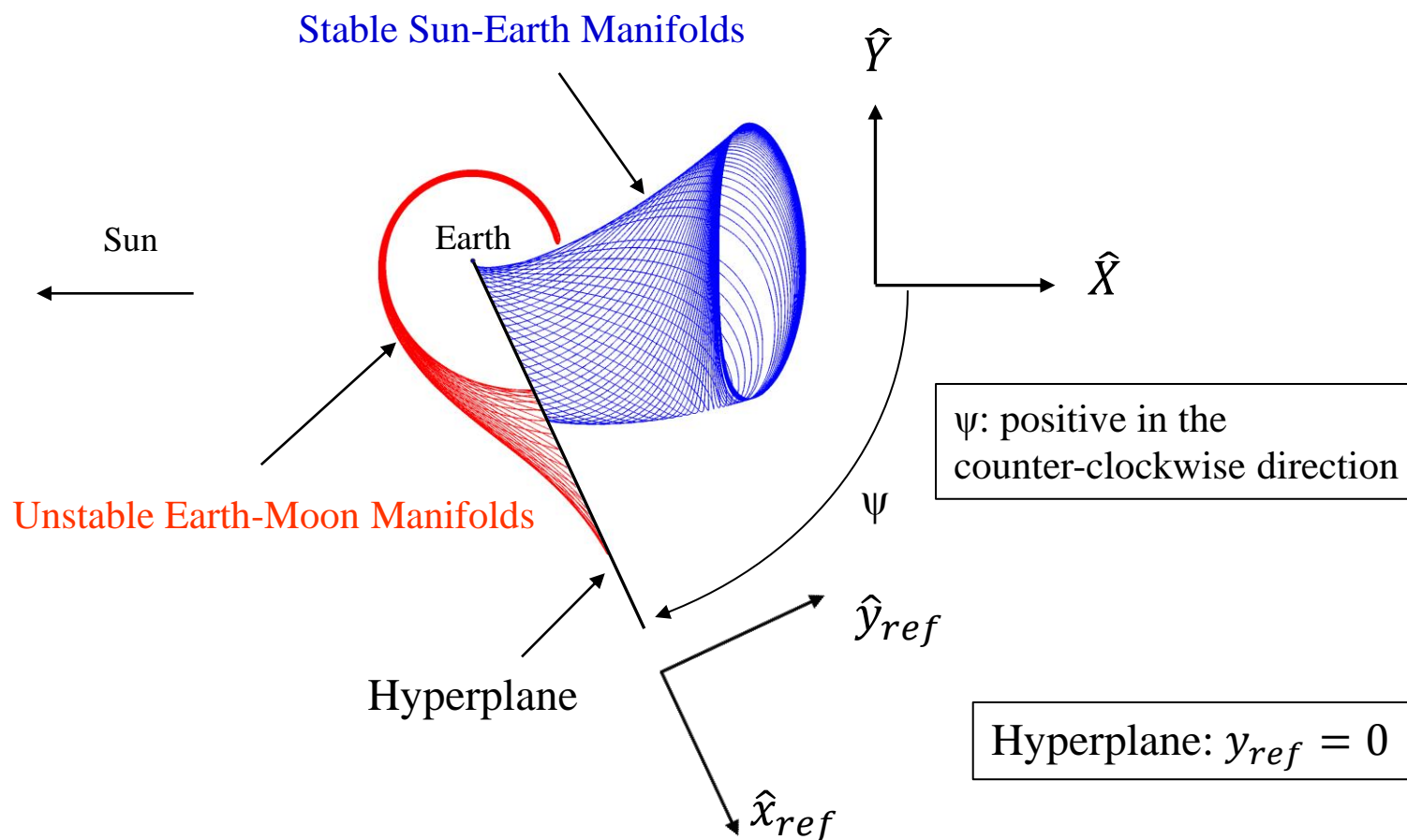
- Scenario 1:
  - Earth-Moon halo orbit to Sun-Earth system
    - Manifold-to-manifold transfers
  - Sun-Earth system to Mars
    - Target ephemeris Mars



- Requirements:
  - Construct manifold-to-manifold transfer scheme
  - Construct Mars targeting scheme

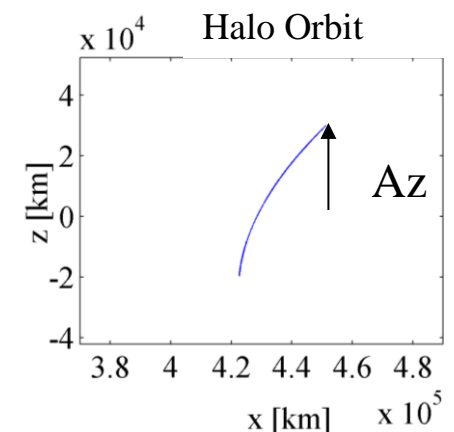
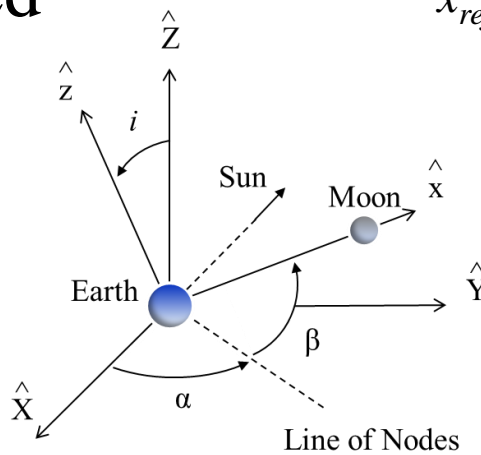
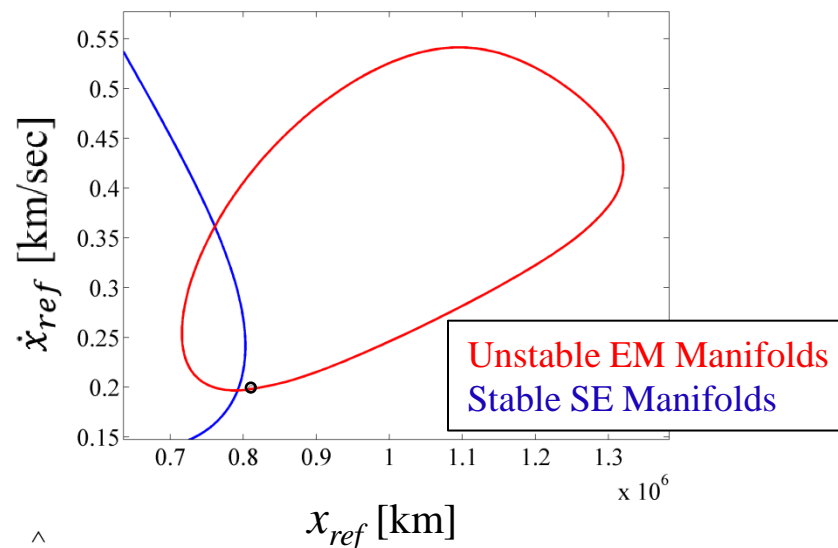


# Defining Reference Frame



# Phase Plots

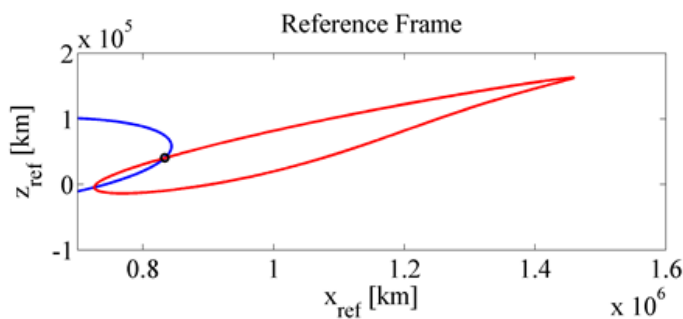
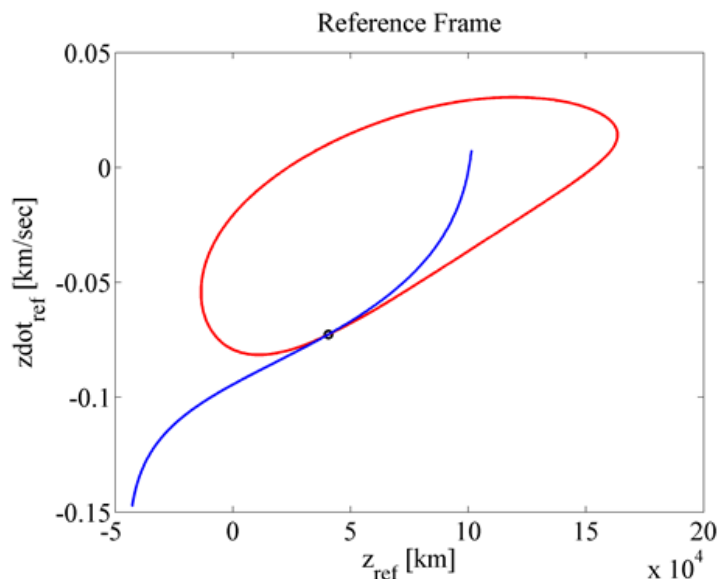
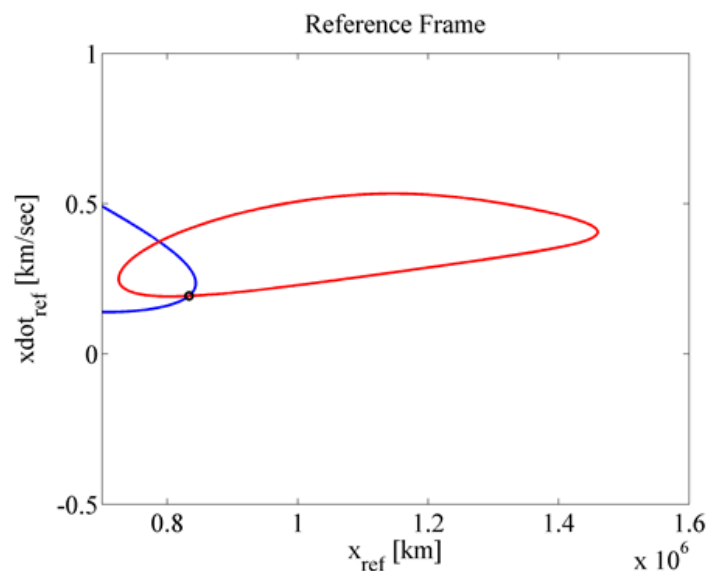
- Three phase plots
  - $\dot{x}_{ref}$  vs  $x_{ref}$
  - $\dot{z}_{ref}$  vs  $x_{ref}$
  - $\dot{z}_{ref}$  vs  $z_{ref}$
  - Fix  $\dot{x}_{ref}$ ,  $x_{ref}$ ,  $z_{ref}$ ,  $\dot{z}_{ref}$
- 5 components fixed
- Jacobi constant
  - Fix  $\dot{y}_{ref}$
- Parameters
  - $\alpha$ ,  $\beta$ ,  $\psi$ , EMaZ, SEaZ





# Phase Plots:

## $\alpha, \beta, \psi, \text{EMAz}, \text{SEAz}$ Corrected

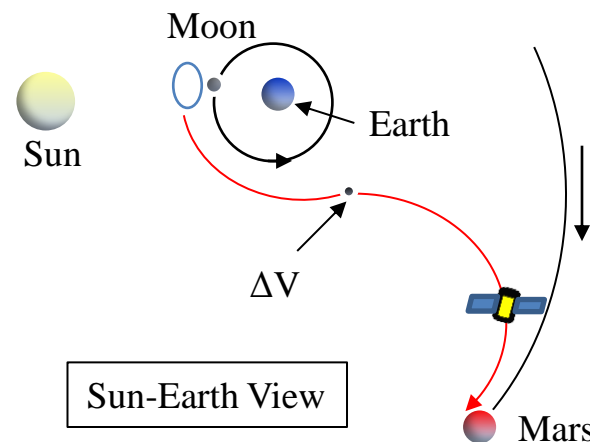
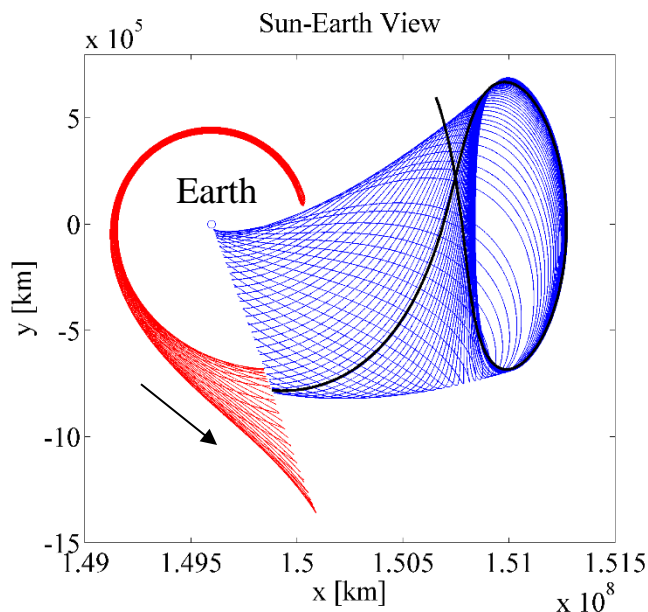


- Maneuver-free manifold-to-manifold transfers computed
  - Red curves and blue curves
    - Intersect at black circle
- Applicable to transfers between  $\text{EML}_2$  and  $\text{SEL}_1/L_2$



# Scenario 1: Sun-Earth Manifold Transfers

- Requirements:
  - Construct manifold-to-manifold transfer scheme
  - Construct Mars targeting scheme



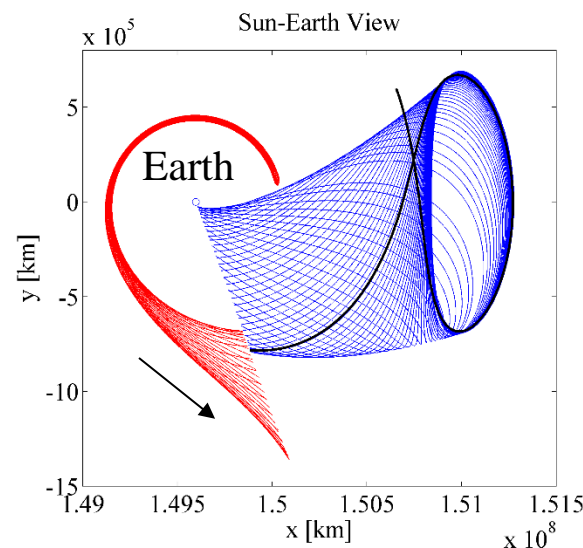




# Scenario 1 Guidelines:

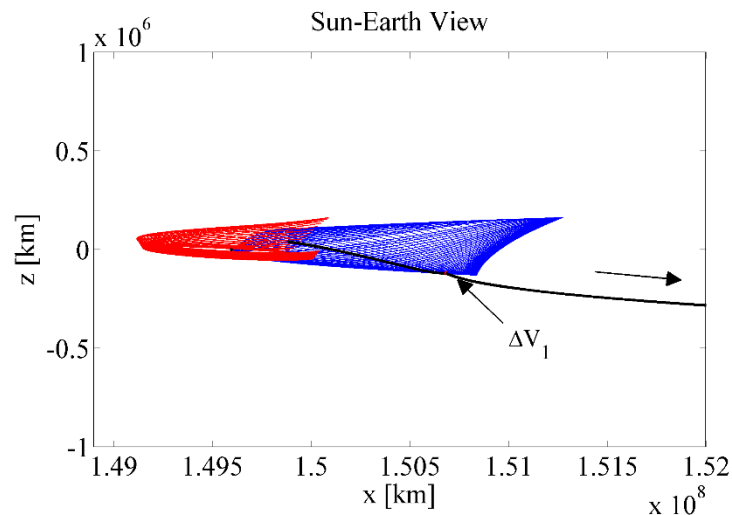
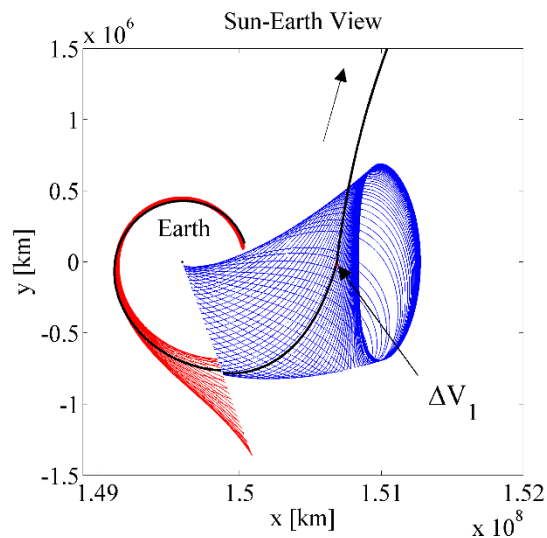
## Sun-Earth Manifold Transfer

- Possible departure dates:
  - Location of the Moon:  $\alpha$ ,  $i$ ,  $\beta$
- Final location of Mars
  - Time-of-flight (TOF): Hohmann transfer
- Targeting Mars
  - Initial guess: Hohmann transfer
    - TOF and  $\Delta V$
  - Multiple shooting method
    - Allow two maneuvers





# Scenario 1 Sample Results: Sun-Earth Manifold Transfer



Departure Date: June 16 2022

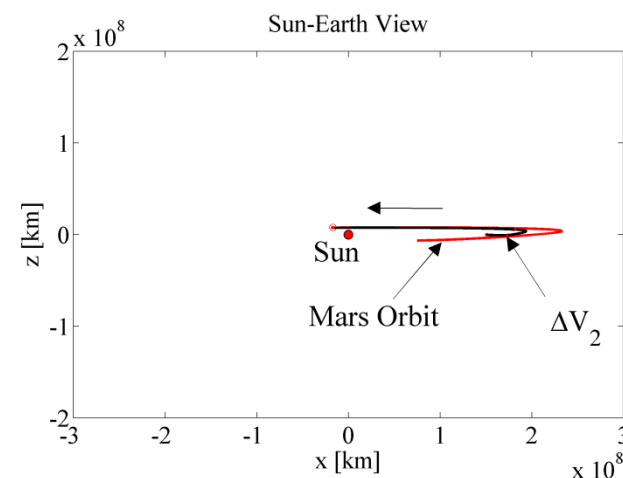
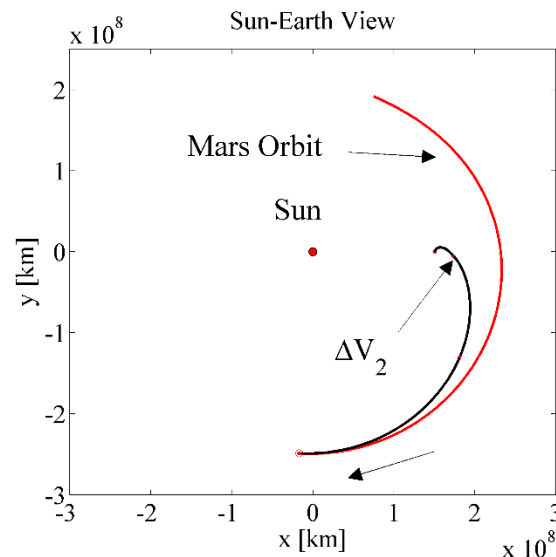
$\Delta V$ : 3.495 km/sec

TOF: 350 days

Planar Hohmann Approx.:

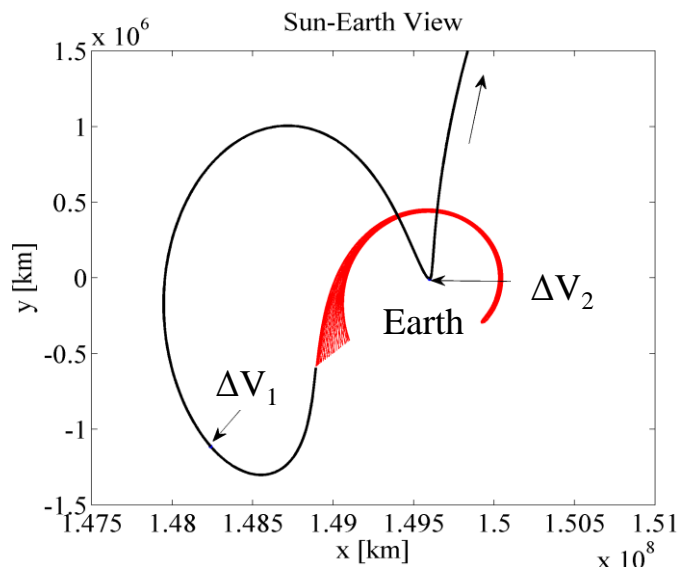
$\Delta V$ : 2.765 km/sec

TOF: 349 days

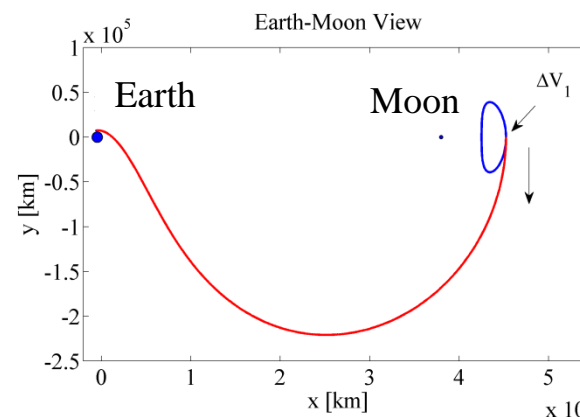


# Additional Scenarios

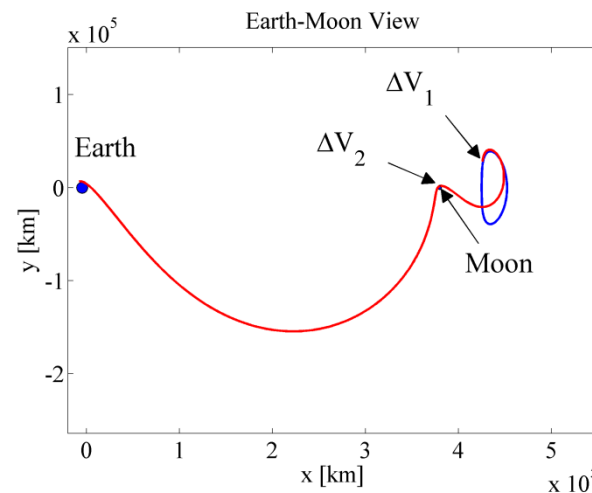
## Scenario 2: Earth-Moon manifold transfers



## Scenario 3: Direct transfers



## Scenario 4: Transfers with lunar flyby



### Development of general procedures

- Total: 4 scenarios
- EML<sub>1</sub>/L<sub>2</sub> departures
- Transfers available every 2 years



# Sample Results: Blended & Higher Fidelity Models

Higher fidelity model:

- Ephemeris: Sun, Earth, Moon, Mars

| Scenario                  | Model     | EMAz [km] | Departure Date | Total $\Delta V$ [km/sec] | TOF [day] |
|---------------------------|-----------|-----------|----------------|---------------------------|-----------|
| SE Manifold Transfer      | Blended   | 25,000    | June 16 2022   | 3.495                     | 350       |
|                           | Ephemeris | 25,000    | June 16 2022   | 3.645                     | 350       |
| EM Manifold Transfer      | Blended   | 25,000    | July 3 2028    | 0.759                     | 380       |
|                           | Ephemeris | 33,000    | July 3 2028    | 0.852                     | 376       |
| Direct Transfer           | Blended   | 25,000    | Nov. 4 2026    | 1.593                     | 272       |
|                           | Ephemeris | 46,000    | Nov. 3 2026    | 1.631                     | 262       |
| Transfer with Lunar Flyby | Blended   | 25,000    | Dec. 1 2028    | 1.150                     | 249       |
|                           | Ephemeris | 27,000    | Dec. 1 2028    | 1.423                     | 249       |



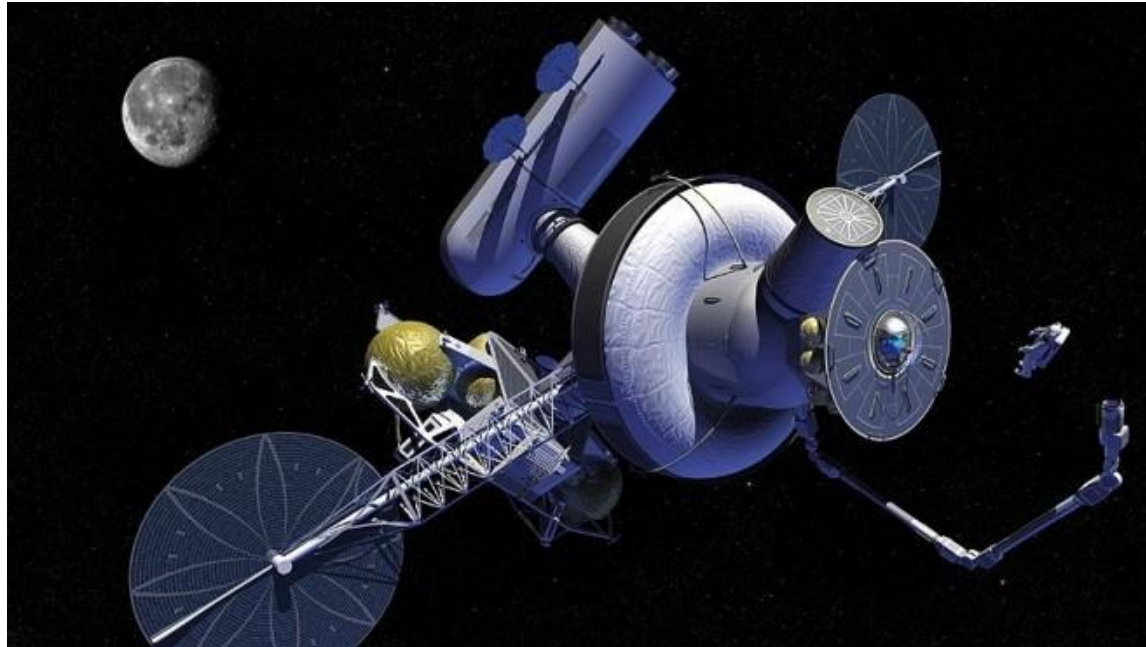
# Concluding Remarks

## Development of general procedure

- Transfers from  $EML_1/L_2$  halo orbits to Mars
  - Blended model constructed
  - Four scenarios introduced
    - Manifold and direct options
  - Maneuver-free transfers between EM and SE systems
  - Results transitioned to higher fidelity model



# Access to Mars from Earth-Moon Libration Point Orbits: Manifold and Direct Options



Suggested EML<sub>2</sub> module  
Image: NASA

## Acknowledgement

Gerald A. Soffen Memorial Fund for the Advancement of  
Space Science Education